

# **Chapter H.3 – Horizontal and Vertical Cooperation**

Competition Policy and Strategy

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English version of my 2020 lecture

# Horizontal and Vertical Cooperation – Basics

- In addition to collusion (101(1) TFEU), there is legal horizontal cooperation
- Guidelines on the applicability of Article 101 of the Treaty on the Functioning of the European Union to horizontal co-operation agreements (2011/C 11/01), par. 20:
  1. Check whether agreement is capable of affecting trade between member states (101(1))
  2. If yes to 1., then “determine the pro-competitive benefits produced by that agreement and to assess whether those pro-competitive effects outweigh the restrictive effects on competition”
- *ibid.*, par. 49: “The application of the exception rule of Article 101(3) is subject to four cumulative conditions, two positive and two negative:”
  - the agreement must contribute to improving the production or distribution of products or contribute to promoting technical or economic progress, that is to say, lead to efficiency gains;
  - the restrictions must be indispensable to the attainment of those objectives (...)
  - consumers must receive a fair share of the resulting benefits (...) so that they are at least compensated for the restrictive effects of the agreement; hence, efficiencies only accruing to the parties to the agreement will not suffice (...)
  - the agreement must not afford the parties the possibility of eliminating competition (...)

# Horizontal and Vertical Cooperation – Basics

- Examples for horizontal cooperation (cf 2011/C 11/01 and 2000/C 118/03)
  - Information exchange
  - Agreements on R&D
  - Production/specialisation agreements
  - Purchasing agreements
  - Commercialisation/joint marketing activities
  - Agreements on standards
- Information exchange (paras. 55 et seq.)
  - Data shared directly or indirectly (e.g., through trade association or market research organization) between competitors
  - Possible efficiency gains: reduction of information asymmetries, benchmarking, inventory management, reduction of consumers' search costs and the improvement of consumers' choice
  - Possible detrimental effects: might facilitate collusion (awareness of competitors' market strategies); depends of characteristics of the market (concentration, transparency, stability, symmetry, complexity) and type of information
  - Possible that the object of the information sharing is actually a cartel

## Horizontal and Vertical Cooperation – Information Exchange

- Cf pp. 362-363 in Tirole (1988)
- Differentiated goods Bertrand duopoly
- Each firm  $i \in \{1, 2\}$  offers own variant
- Demand for variant  $i$ :  $q_i(p_i, p_j) = a - bp_i + dp_j$  with  $0 < d < b$  (see also Ch. G).
- Constant marginal cost of production
  - Marginal cost  $c_2$  common knowledge
  - Marginal cost  $c_1$  firm 1's private information; either low ( $c_1 = c_L$ ) or high ( $c_2 = c_H$ ).
  - Firm 2's beliefs  $\Pr(c_1 = c_L) = y$  (accordingly,  $\Pr(c_1 = c_H) = 1 - y$ ). Firm 2 thus expects 1's marginal cost:

$$c_1^e = yc_L + (1 - y)c_H.$$

- Both firms are risk-neutral
- Let  $p_1^L$  and  $p_1^H$  be firm 1's price for  $c_1 = c_L$  and  $c_2 = c_H$ , respectively.

## Horizontal and Vertical Cooperation – Information Exchange

- From firm 1's maximization problem,

$$\max_{p_1} \pi_1(p_1, p_2) = (p_1 - c_1)(a - bp_1 + dp_2),$$

- we get firm 1's reaction function

$$p_1(p_2) = \frac{a + dp_2 + bc_1}{2b}.$$

- Thus, firm 2 expects firm 1's best response:

$$\hat{p}_1^e(p_2) = yp_1^L + (1 - y)p_1^H \tag{1}$$

$$= y \left( \frac{a + dp_2 + bc_L}{2b} \right) + (1 - y) \left( \frac{a + dp_2 + bc_H}{2b} \right) \tag{2}$$

$$= \frac{a + dp_2 + bc_1^e}{2b}. \tag{3}$$

## Horizontal and Vertical Cooperation – Information Exchange

- From firm 2's optimality condition,

$$\begin{aligned}\max_{p_2} \mathbb{E}(\pi_2(p_1, p_2)) &= y(p_2 - c_2)(a - bp_2 + dp_1^L) + (1 - y)(p_2 - c_2)(a - bp_2 + dp_1^H) \\ &= (p_2 - c_2)(a - bp_2 + dp_1^e),\end{aligned}$$

- with  $p_1^e = yp_1^L + (1 - y)p_1^H$ , we get firm 2's reaction function:

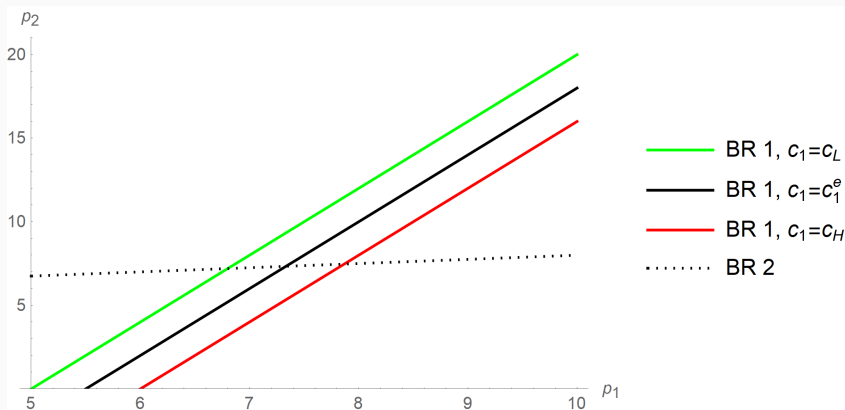
$$p_2(p_1^e) = \frac{a + dp_1^e + bc_2}{2b}. \quad (4)$$

- Using (3) and (4), we get firm 2's equilibrium price

$$p_2^* = \frac{2ab + 2b^2c_2 + ad + bdc_1^e}{4b^2 - d^2}.$$

## Horizontal and Vertical Cooperation – Information Exchange

- Firm 2 expects an “average” best response function that lies between firm 1’s actual reaction functions.



**Figure 1:** Best response functions with  $a = 10$ ,  $b = 1$ ,  $d = 0.5$ ,  $c_2 = 1$ ,  $c_L = 0$ ,  $c_H = 2$  and  $y = 0.5$ , such that  $c^e = 1$ .

## Horizontal and Vertical Cooperation – Information Exchange

- Let  $p_2^L$  and  $p_2^H$  be firm 2's prices for  $c_1 = c_L$  and  $c_1 = c_H$ , respectively, in case of full information.
- Firm 2's equilibrium price with uncertainty,  $p_2^*$  (intersection black and dotted line in Figure 1)
  - When firm 1 has low marginal cost, firm 2 sets a higher price than with full information ( $p_2^* > p_2^L$ , intersection green and dotted line in Figure 1)
  - When firm 1 has high marginal cost, firm 2 sets a lower price than with full information ( $p_2^* < p_2^H$ , intersection red and dotted line in Figure 1)
- Assume that the firms are allowed to exchange information before they compete in the market.
  - When marginal cost are low, firm 1 has no incentive to reveal its type as this would lead to a price reduction of firm 2 ( $p_2^* > p_2^L$ , see above), i.e., a reduction in firm 1's profits compared to the outcome with uncertainty.
  - When marginal cost are high, firm 1 has an incentive to reveal its type as this would lead to an increase in firm 2's price ( $p_2^* < p_2^H$ , see above), i.e., an increase in firm 1's profits compared to the outcome with uncertainty.

# Horizontal and Vertical Cooperation – Information Exchange

- Case 1: verifiable information
  - When  $c_1 = c_L$ : firm 1 has no incentive to reveal information about its marginal cost because it pays off to keep firm 2 uninformed.
  - When  $c_1 = c_H$ : firm 1 truthfully reveals its cost type to firm 2.
  - Firm 2 knows that firm 1 only reveals its type when marginal costs are high. If firm 2 receives no information about firm 1's cost type, it knows that firm 1 has low cost!
  - Effect of information exchange is unclear as higher prices are possible.
- Case 2: non-verifiable information
  - When  $c_1 = c_L$ : firm 1 benefits from firm 2 believing that firm 1 has high marginal costs
  - When  $c_1 = c_H$ : firm 1 has an incentive to reveal its cost type.
  - Firm 1 would always claim to have high marginal costs, irrespective of its true cost type (Pooling-Equilibrium)
  - Firm 2 cannot verify the information on firm 1's cost type and anticipates that it will receive information that firm 1 had high cost  $\Rightarrow$  information exchanged are not credible

# Horizontal and Vertical Cooperation – Research and Development Agreements

- Research joint ventures (RJVs, paras. 111 et seq. in 2011/C 11/01)
  - Outsourcing certain R&D activities
  - Joint improvement of existing technologies
  - Cooperation in research and development and marketing
  - Cooperation agreement or jointly controlled company
  - May also affect “future” product markets
  - Potentially slows down (!) R&D activity (see next slides) or leads to collusion

# Horizontal and Vertical Cooperation – Research and Development Agreements

- RJV-model; first w/o RJV.
- Stage 1
  - Firm  $i \in \{1, 2\}$  chooses research activity  $x_i \in \mathbb{R}_+$ .
  - Marginal cost  $c_i = c - x_i - \beta x_j$ , with  $\beta \in [0, 1]$  measuring the spillover of R&D activities between firms  $\Rightarrow$  R&D-activity of firm  $i$  also reduces  $j$ 's marginal cost (free-riding; increases in  $\beta$ ).
  - Firm  $i$ 's R&D-cost are  $x_i^2$
- Stage 2
  - Firms compete in quantities (Cournot).
  - Demand function  $q(p) = a - p$ .
- Backwards induction

$$\max_{q_i} \pi_i(q_i, q_j, x_i, x_j) \quad \forall i \in \{1, 2\} \Rightarrow q_i(x_i, x_j) = \frac{a - 2c_i(x_i, x_j) + c_j(x_i, x_j)}{3}.$$

- Stage 2 profits:  $\pi_i(x_i, x_j) = \left( \frac{a - 2c_i(\cdot) + c_j(\cdot)}{3} \right)^2 - x_i^2$ .

# Horizontal and Vertical Cooperation – Research and Development Agreements

- Optimality condition stage 1

$$\max_{x_i} \pi_i(x_i, x_j) = \left( \frac{a - c + (2 - \beta)x_i - (1 - 2\beta)x_j}{3} \right)^2 - x_i^2.$$

- Gives best response function

$$x_i(x_j) = \frac{(2 - \beta)(a - c + x_j(2\beta - 1))}{(5 - \beta)(1 + \beta)}.$$

- If  $\beta > 0.5$ , we have  $\frac{dx_i}{dx_j} > 0$ : research activity **strategic complements**.
- If  $\beta < 0.5$ , we have  $\frac{dx_i}{dx_j} < 0$ : research activity **strategic substitutes**.
- Equilibrium research activity:

$$x_i^* = \frac{(\beta - 2)(a - c)}{7 + (\beta - 1)\beta}.$$

- We have  $\frac{dx_i^*}{d\beta} < 0$  for all  $\beta \in [0, 1]$ . The higher  $\beta$  the lower the research activity in equilibrium due to more severe free-riding

# Horizontal and Vertical Cooperation – Research and Development Agreements

- Suppose that firms install RJV
- Firms continue to compete on product market, but maximize joint profits when choosing research activity  $x_i$ :

$$\max_{x_i, x_j} \pi_i(\cdot) + \pi_j(\cdot) = \left( \frac{a - c + (2 - \beta)x_i - (1 - 2\beta)x_j}{3} \right)^2 + \left( \frac{a - c + (2 - \beta)x_j - (1 - 2\beta)x_i}{3} \right)^2 - (x_i^2 + x_j^2).$$

- We get equilibrium research activity with RJV

$$x_i^{\text{RJV}} = \frac{(a - c)(\beta + 1)}{(2 - \beta)(4 + \beta)}.$$

- Comparison of  $x_i^*$  and  $x_i^{\text{RJV}}$  shows that effect of RJV on research activity is ambiguous
- Two effects:
  - RJV internalizes spillovers, thereby reducing incentives for free-riding and increasing research activity
  - RJV decreases “pressure” to innovate of competitors

# Horizontal and Vertical Cooperation – Research and Development Agreements

- RJV increases research activity if  $\beta > 0.5$ .

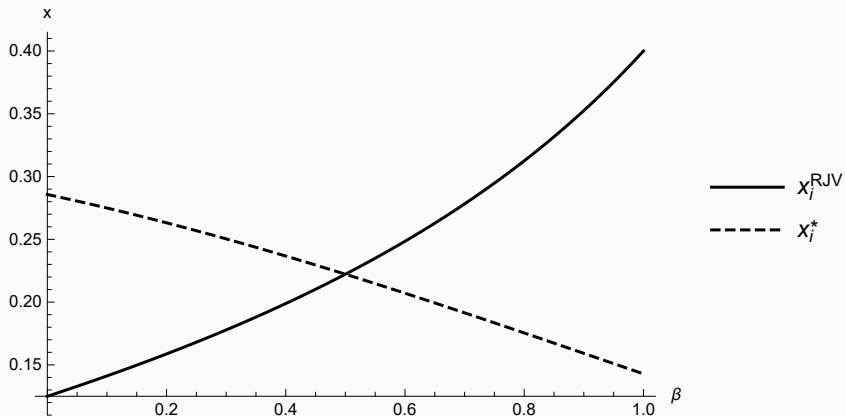


Figure 2: Research activity w/o RJV,  $x_i^*$ , and with RJV,  $x_i^{RJV}$ , with  $a - c \equiv 1$ .

# Horizontal and Vertical Cooperation – Research and Development Agreements

- Suppose that firms can increase  $\beta$  to 1 in RJV (e.g., disclosure of research)
- Equilibrium research intensity then is  $0.4(a - c)$  such that marginal costs are  $c_i^{\text{RJV}} = \frac{9c-4a}{5}$
- Equilibrium output and price on stage 2 resp. reads  $q_i^{\text{RJV}} = 0.6(a - c)$  and  $p^{\text{RJV}} = 1.2c - 0.2a$
- Market price w/o RJV (exogenous  $\delta \in [0, 1]$ ) reads  $p^* = a + \frac{6(a-c)}{2\beta+\beta^2-8}$ , such that  $p^* > p^{\text{RJV}}$ .
- RJV increases consumer surplus and welfare

## Horizontal and Vertical Cooperation – Further Examples

- Production/specialisation agreements (paras. 150 et seq. in 2011/C 11/01)
  - Production by one or more companies, separate joint venture
  - Horizontal or vertical
  - Realize gains from specialization
  - Might facilitate collusion or foreclosure
- Purchasing agreements (paras. 194 et seq., *ibid.*)
  - Purchase (intermediate) products jointly
  - Creation of buyer power, reduce input costs/increase quality, etc.
  - Horizontal or vertical
  - Might facilitate collusion or foreclosure
- Commercialisation/joint marketing activities (paras. 225 et seq., *ibid.*)
  - Joint retailing or marketing activities
  - Might facilitate collusion or foreclosure
- Agreements on standards (paras. 257 et seq., *ibid.*)
  - Establish standards for existing and future products, production processes, etc.
  - Only problematic if reduction in competition between different technologies

# Horizontal and Vertical Cooperation – Purchasing Agreements and Buyer Power

- Firms can improve/establish buyer power by installing purchasing agreement
- Examples of buyer power
  - Listing fees
  - Slotting allowances
  - Advertising grants
  - Exclusivity clauses

# Horizontal and Vertical Cooperation – Purchasing Agreements and Buyer Power

- Purchasing agreement: (downstream) firms become monopolistic buyer  $\Rightarrow$  monopsony (e.g., pp. 77–78 in Varian, 1981)
- Assumptions:
  - Homogeneous good supplied by multiple, price-taking downstream firms
  - Downstream firms purchase intermediate product at (wholesale) price  $w$  and sell good to final customers at (retail) price  $p$ . Demand reads  $q(p) = a - p$ .
  - Upstream firms are price-takers as well
  - Cost function upstream reads  $c(q) = q^2$ .
- Case 1: no buyer power
  - On downstream-level, we have  $p = w$ .
  - Supply of upstream firm

$$\max_q \pi_U = wq - q^2 \Rightarrow w = 2q.$$

- In equilibrium, we have  $p = 2q$  (retail price is equal to marginal cost upstream), such that  $q_{\text{Case 1}} = \frac{a}{3}$ .

# Horizontal and Vertical Cooperation – Purchasing Agreements and Buyer Power

- Case 2: downstream firms establish purchasing agreement and behave as one monopsonistic buyer
  - Upstream, we still have  $w = 2q$ .
  - Downstream firms internalize increasing marginal cost/increase in wholesale prices such that

$$\max_q \pi_D = pq - \underbrace{2q^2}_{w(q)q} \Rightarrow p = \frac{q}{4}.$$

- Equilibrium quantity decreases to  $q_{\text{Case 2}} = \frac{a}{5}$
  - Monopsony decreases quantity/increases retail prices. Downstream profits increase from zero to  $\frac{2a^2}{5}$ .
- Here: buyer power reduces welfare
  - Caveats
    1. Results are driven by assumption of increasing marginal cost
    2. Price-taking behavior upstream.

# Horizontal and Vertical Cooperation – Purchasing Agreements and Buyer Power

- Bilateral monopoly
- Suppose that upstream marginal costs are a constant,  $c$
- Efficient outcome obtains when retail price is equal to monopoly price  $\frac{a}{2}$ , with ensuing profits  $\pi_M = \frac{a^2}{4}$ 
  - Bargaining over one indivisible unit (i.e., the monopoly quantity)
  - Fixed Fee  $T$  charged by upstream firm (e.g., part of two-part tariff; see future lectures and IO class!)
  - Disagreement profits upstream are  $c$  (e.g., sell to an outside market for price equals marginal costs)
  - Disagreement profits downstream are zero
- In equilibrium,  $T \in [c, \pi_M]$ 
  - Any  $T < c$  will lead to upstream firm breaking up negotiations as the firm would have to sell below marginal cost
  - Any  $T > \pi_M$  will lead to downstream firm breaking up negotiations as the firm would make losses
- Upstream and downstream firm negotiate how to “split the pie”!

# Horizontal and Vertical Cooperation – Slotting Allowances

- Model of slotting allowances of Shaffer (1991, RAND).
  - Perfectly competitive upstream producers of homogeneous good, constant marginal cost  $c$
  - $\mathcal{N} = \{1, 2\}$  retailers downstream that sell good to final consumers, no further costs
  - Consumers perceive retailers as differentiated (e.g., location)
  - Demand of retailer  $i \in \mathcal{N}$

$$q_i(p_i, p_j) = \frac{a - (1 + \gamma)p_i + \gamma p_j}{2}.$$

- If  $p_i$  increases by one unit, sales of  $i$  decrease by  $1 + \gamma$ , whereas sales of  $j$  increase by  $\gamma$ . For  $\gamma = 0$  ( $\gamma \rightarrow \infty$ ) retailers are independent (perfect substitutes).
- Timing
  1. Producers sets wholesale price  $w_i$  or two-part tariff ( $w_i, T_i$ ) for each retailer  $i$ .
  2. Each retailer chooses from which producer to buy from
  3. retailers compete

# Horizontal and Vertical Cooperation – Slotting Allowances

- Case 1:  $T = 0$

- Backwards induction: 3rd stage, competition between retailers for given  $w_i$

$$\max_{p_i} \pi_i(p_i, p_j, w_i) = (p_i - w_i) \frac{a - (1 + \gamma)p_i + \gamma p_j}{2} \quad \forall i \in \{1, 2\}, i \neq j.$$

- yields equilibrium retail prices

$$p_i(w_i, w_j) = \frac{a(2 + 3\gamma) + (1 + \gamma)(2w_i(1 + \gamma) + w_j\gamma)}{4 + 8\gamma + 3\gamma^2}.$$

- 2nd and 1st stage, retailer  $i$  buys from producer such that

$$\max_{w_i} \{ \pi_i(w_i, w_j) = (p_i(w_i, w_j) - w_i)q_i(p_i(w_i, w_j), p_j(w_i, w_j)) : (w_i - c)q_i(p_i(w_i, w_j), p_j(w_i, w_j)) = 0 \}$$

- Zero-profit condition (constraint) due to perfect competition upstream.
- From Langrangean, we get  $w_i = c$  for all  $i$  in equilibrium.
- Retailer  $i$ 's prices in equilibrium:

$$p_i^* = \frac{a + c(1 + \gamma)}{2 + \gamma}.$$

# Horizontal and Vertical Cooperation – Slotting Allowances

- Case 2: Two-Part Tariffs ( $T \neq 0$  possible).

- Competition downstream as in Case 1:

$$\max_{p_i} = (p_i - w_i)q_i(p_i, p_j) \Rightarrow (p_i - w_i)\frac{\partial q_i}{\partial p_i} + q_i = 0 \Leftrightarrow q_i + p_i\frac{\partial q_i}{\partial p_i} = w_i\frac{\partial q_i}{\partial p_i}, \quad (5)$$

- such that

$$p_i(w_i, w_j) = \frac{a(2 + 3\gamma) + (1 + \gamma)(2w_i(1 + \gamma) + w_j\gamma)}{4 + 8\gamma + 3\gamma^2}.$$

- Using  $(w_i, T_i)$ , retailer  $i$  buys from producer such that

$$\max_{w_i, T_i} \left\{ \pi_i(\cdot) = \right. \\ \left. (p_i(w_i, w_j) - w_i)q_i(p_i(w_i, w_j), p_j(w_i, w_j)) - T_i : (w_i - c)q_i(p_i(w_i, w_j), p_j(w_i, w_j)) + T_i = 0 \right\}.$$

- Lagrangean:

$$\mathcal{L}(w_i, T_i, \lambda) = (p_i(w_i, w_j) - w_i)q_i(p_i(w_i, w_j), p_j(w_i, w_j)) - T_i + \\ \lambda((w_i - c)q_i(p_i(w_i, w_j), p_j(w_i, w_j)) + T_i).$$

## Horizontal and Vertical Cooperation – Slotting Allowances

- Case 2: Two-Part Tariffs ( $T \neq 0$  possible).

- From  $\frac{\partial \mathcal{L}}{\partial T_i} = 0$ , we have  $\lambda = 1$ .
- Thus,  $\frac{\partial \mathcal{L}}{\partial w_i} = 0$  is equivalent to

$$\left[ (p_i - c) \frac{\partial q_i}{\partial p_i} + q_i(\cdot) \right] \frac{\partial p_i}{\partial w_i} + (p_i - c) \frac{\partial q_i}{\partial p_j} \frac{\partial p_j}{\partial w_i} = 0. \quad (6)$$

- Substituting (5) into (6), we get

$$(w_i - c) \underbrace{\frac{\partial q_i}{\partial p_i} \frac{\partial p_i}{\partial w_i}}_{<0} + (p_i - c) \underbrace{\frac{\partial q_i}{\partial p_j} \frac{\partial p_j}{\partial w_i}}_{>0} = 0. \quad (7)$$

- In equilibrium, we must have  $w_i > c$  and  $T_i < 0$ , for (7) to be satisfied:
  - If  $w_i = c$ , second term in (7) has to be zero as well. However, the term is positive. Hence,  $w_i \neq c$ .
  - If  $w_i < c$ , first term in (7) is positive, such that second term must be negative. This requires that  $p_j < c$ , which is only possible for  $T_j < 0$ . Otherwise, retailer would incur losses. However, for  $w_i < c$  and  $T_i < 0$ , we have losses upstream. Thus, we must have  $w_i > c$ .
  - For  $w_i > c$ , we must have  $T_i < 0$  since otherwise there would be profits upstream.

# Horizontal and Vertical Cooperation – Slotting Allowances

- Case 2: Two-Part Tariffs ( $T \neq 0$  possible).
  - Computation (fyi):
    - For  $\lambda = 1$ , we have

$$\frac{\partial \mathcal{L}}{\partial w_1} = \frac{(\gamma + 1) (\gamma^2(a(3\gamma + 2) + \gamma(\gamma + 1)w_2) + c(\gamma + 2)(3\gamma + 2)(\gamma(\gamma + 4) + 2) - 4(\gamma + 1)^2(\gamma(\gamma + 4) + 2)w_1)}{2(\gamma + 2)^2(3\gamma + 2)^2} \stackrel{!}{=} 0.$$

- Symmetry  $w_1 = w_2$  implies

$$w_i^{2PT} = \frac{a\gamma^2 + c(2 + \gamma)(2 + \gamma(4 + \gamma))}{(1 + \gamma)(4 + \gamma(6 + \gamma))}.$$

- This implies

$$p_i^{2PT} = \frac{2a(1 + \gamma) + c(2 + \gamma(4 + \gamma))}{4 + \gamma(6 + \gamma)}.$$

- Equilibrium demand reads

$$q_i^{2PT} = \frac{(a - c)(2 + \gamma(4 + \gamma))}{8 + 2\gamma(6 + \gamma)}.$$

- Using zero-profit condition, we get  $T_i < 0$  such that:

$$(w_i^{2PT} - c)q_i^{2PT} + T_i = 0 \Leftrightarrow T_i^{2PT} = -\frac{(a - c)^2\gamma^2(2 + \gamma(4 + \gamma))}{2(1 + \gamma)(4 + \gamma(6 + \gamma))^2} < 0.$$

## Horizontal and Vertical Cooperation – Slotting Allowances

- Compared to linear prices, two-part tariffs lead to
  - Increasing wholesale prices  $w$
  - Producers paying slotting allowances (technically,  $T < 0$  is paid by retailers)
  - Profit  $(w_i - c)q_i > 0$  upstream is extracted with fixed fee/slotting allowance
  - Retail prices increase ( $p_i^{2PT} > p_i^*$ , cf Proposition 8 in Shaffer (1991)).