

## Behind the Supply Curve: Inputs and Costs

## WHAT YOU <br> WILL LEARN IN THIS CHAPTER

- The importance of the firm's production function, the relationship between quantity of inputs and quantity of output
- Why production is often subject to diminishing returns to inputs
- The various types of costs a firm faces and how they generate the firm's marginal and average cost curves
- Why a firm's costs may differ in the short run versus the long run
- How the firm's technology of production can generate increasing returns to scale


## The Production Function

- A production function is the relationship between the quantity of inputs a firm uses and the quantity of output it produces.
- A fixed input is an input whose quantity is fixed for a particular period and cannot be varied.
- A variable input is an input whose quantity the firm can vary at any time.


## Inputs and Output

- The long run is the period in which all inputs can be varied.
- The short run is the period in which at least one input is fixed.
- The total product curve shows how the quantity of output depends on the quantity of the variable input, for a given quantity of the fixed input.


## Production Function and TP Curve for George and Martha's Farm

Quantity of
wheat
(bushels)
Adding a $7^{\text {th }}$ worker leads to an increase in output of only 7 bushels

| Quantity of | Quantity | MP of labor |
| :---: | :---: | :---: |
| labor $L$ | of wheat $Q$ | $M P L=\Delta Q / \Delta L$ |
| (worker) | (bushels) | (bushels per worker) |



Although the total product curve in the figure slopes upward along its entire length, the slope isn't constant: as you move up the curve to the right, it flattens out due to changing marginal product of labor.

## Marginal Product of Labor

- The marginal product of an input is the additional quantity of output that is produced by using one more unit of that input.

| Marginal |
| :--- |
| product |
| of labor |$=\frac{\text { Change in quantity of output }}{\text { Change in quantity of labor }}=$| Change in quantity of |
| :---: |
| output generated by one |
| additional unit of labor |

$$
M P L=\Delta Q / \Delta L
$$

## GLOBAL COMPARISON: Wheat Yields Around The World

- The disparity between France and the United States is striking, given that they are both wealthy countries with comparable agricultural technology.
- In the United States, farmers receive payments from the government to supplement their incomes, but European farmers benefit from price floors.
- In poor countries like Uganda and Ethiopia, foreign aid can lead to significantly depressed yields.
- Foreign aid from wealthy countries ha often taken the form of surplus food, which depresses local market prices,
 severely hurting the local agriculture that poor countries normally depend on.


## Diminishing Returns to an Input

- There are diminishing returns to an input when an increase in the quantity of that input, holding the levels of all other inputs fixed, leads to a decline in the marginal product of that input.
- The following marginal product of labor curve illustrates this concept clearly.


## Marginal Product of Labor Curve



Here, the first worker employed generates an increase in output of 19 bushels, the second worker generates an increase of 17 bushels, and so on...

## Total Product, Marginal Product, and the Fixed Input



This shift also implies that the marginal
With more land, each worker can produce more wheat. So an increase in the fixed input shifts the total product curve up from $T P_{10}$ to $T P_{20}$. product of each worker is higher when the farm is larger. As a result, an increase in acreage also shifts the marginal product of labor curve up from $M P L_{10}$ to $M P L_{20}$.

## Pitfalls

## What's a Unit?

- The marginal product of labor (or any other input) is defined as the increase in the quantity of output when you increase the quantity of that input by one unit.
- What do we mean by a "unit" of labor? Is it an additional hour of labor, an additional week, or a person-year?
- The answer is that it doesn't matter, as long as you are consistent.
- One common source of error in economics is getting units confused-say, comparing the output added by an additional hour of labor with the cost of employing a worker for a week.
- Whatever units you use, always be careful that you use the same units throughout your analysis of any problem.


## From the Production Function to Cost Curves

- A fixed cost is a cost that does not depend on the quantity of output produced. It is the cost of the fixed input.
- A variable cost is a cost that depends on the quantity of output produced. It is the cost of the variable input.


## Total Cost Curve

- The total cost of producing a given quantity of output is the sum of the fixed cost and the variable cost of producing that quantity of output.

$$
T C=F C+V C
$$

- The total cost curve becomes steeper as more output is produced due to diminishing returns.


## Total Cost Curve for George and Martha's Farm



## ECONOMICS IN ACTION

## The Mythical Man-Month

- "Adding another programmer on a project actually increases the time to completion."
- The source of the diminishing returns lies in the nature of the production function for a programming project: Each programmer must coordinate his or her work with that of all the other programmers on the project, leading to each person spending more and more time communicating with others as the number of programmers increases.


## ECONOMICS IN ACTION: The Mythical Man-Month



Marginal product of labor (lines per programmer)


Quantity of labor (programmers)

## Two Key Concepts: Marginal Cost and Average Cost

$$
\begin{aligned}
& \text { Marginal cost }=\frac{\text { Change in total cost }}{\text { Change in quantity of output }}=\begin{array}{c}
\text { Change in total cost } \\
\text { generated by one } \\
\text { additional unit of } \\
\text { output }
\end{array} \\
& M C=\Delta T C / \Delta Q
\end{aligned}
$$

As in the case of marginal product, marginal cost is equal to rise (the increase in total cost) divided by run (the increase in the quantity of output).

## Costs at Selena's Gourmet Salsas

## table 11-1 Costs at Selena's Gourmet Salsas

Quantity of
salsa Q (cases)

0

Fixed cost FC
\$108

108
12
$108 \quad 48$
108

108
108
108
432
108
588
768
972

10
108
1,200

Total cost $T C=F C+V C$

Marginal cost
of case
$M C=\Delta T C / \Delta Q$\$1236








1,080
228
1,308

## Total Cost and Marginal Cost Curves for Selena's Gourmet Salsas

(a) Total Cost
(b) Marginal Cost


## Why is the Marginal Cost Curve Upward Sloping?

- The marginal cost curve is upward sloping because there are diminishing returns to inputs in this example. As output increases, the marginal product of the variable input declines.
- This implies that more and more of the variable input must be used to produce each additional unit of output as the amount of output already produced rises.
- And since each unit of the variable input must be paid for, the cost per additional unit of output also rises.


## Average Cost

- Average total cost, often referred to simply as average cost, is total cost divided by quantity of output produced.

$$
A T C=T C / Q=(\text { Total Cost }) /(\text { Quantity of Output })
$$

- A U-shaped average total cost curve falls at low levels of output, then rises at higher levels.


## Average Cost

- Average fixed cost is the fixed cost per unit of output.

$$
A F C=F C / Q=(\text { Fixed Cost) } / \text { (Quantity of Output })
$$

- Average variable cost is the variable cost per unit of output.

$$
A V C=V C / Q=\text { (Variable Cost) / (Quantity of Output) }
$$

## Average Total Cost Curve

- Increasing output, therefore, has two opposing effects on average total cost-the spreading effect and the diminishing returns effect:
- The spreading effect: the larger the output, the greater the quantity of output over which fixed cost is spread, leading to lower the average fixed cost
- The diminishing returns effect: the larger the output, the greater the amount of variable input required to produce additional units leading to higher average variable cost


## Average Costs for Selena's Gourmet Salsas

table 11-2 Average Costs for Selena's Gourmet Salsas

| Quantity <br> of salsa <br> Q (cases) | Total <br> cost <br> TC | Average total <br> cost of case <br> ATC $=\boldsymbol{T C} / \mathbf{Q}$ |
| :---: | :---: | :---: |
| 1 | $\$ 120$ | $\$ 120.00$ |
| 2 | 156 | 78.00 |
| 3 | 216 | 72.00 |
| 4 | 300 | 75.00 |
| 5 | 408 | 81.60 |
| 6 | 540 | 90.00 |
| 7 | 696 | 99.43 |
| 8 | 876 | 109.50 |
| 9 | 1,080 | 120.00 |
| 10 | 1,308 | 130.80 |


| Average fixed |
| :---: |
| cost of case |
| $\boldsymbol{A F C}=\boldsymbol{F C} / \boldsymbol{Q}$ |
| $\$ 108.00$ |
| 54.00 |
| 36.00 |
| 27.00 |
| 21.60 |
| 18.00 |
| 15.43 |
| 13.50 |
| 12.00 |
| 10.80 |

Average variable cost of case AVC $=V C / Q$
\$12.00
24.00
36.00
48.00
60.00
72.00
84.00
96.00
108.00
120.00

## Average Total Cost Curve for Selena's Gourmet Salsas



## Putting the Four Cost Curves Together

Note that:

1. Marginal cost is upward sloping due to diminishing returns.
2. Average variable cost also is upward sloping, but is flatter than the marginal cost curve.
3. Average fixed cost is downward sloping because of the spreading effect.
4. The marginal cost curve intersects the average total cost curve from below, crossing it at its lowest point. This last feature is our next subject of study.

## Marginal Cost \& Average Cost Curves for Selena's Gourmet Salsas

The bottom of the $U$ curve is at the level of output at which the marginal cost curve crosses the average total cost curve from below.

Is this an accident? No!

Cost of case


## General Principles that Are Always True About a Firm's Marginal and Average Total Cost Curves

- The minimum-cost output is the quantity of output at which average total cost is lowest-the bottom of the U-shaped average total cost curve.
- At the minimum-cost output, average total cost is equal to marginal cost.
- At output less than the minimum-cost output, marginal cost is less than average total cost and average total cost is falling.
- And at output greater than the minimum-cost output, marginal cost is greater than average total cost and average total cost is rising.


## The Relationship Between the Average Total Cost and the Marginal Cost

 CurvesCost of unit


Quantity
When marginal cost equals average total cost, we must be at the bottom of the $U$, because only at that point is average total cost neither falling nor rising.

## Does the Marginal Cost Curve Always Slope Upward?

- In practice, marginal cost curves often slope downward as a firm increases its production from zero up to some low level, sloping upward only at higher levels of production.
- This initial downward slope occurs because a firm that employs only a few workers often cannot reap the benefits of specialization of labor.
- This specialization can lead to increasing returns at first, and so to a downward-sloping marginal cost curve.
- Once there are enough workers to permit specialization, however, diminishing returns set in.


## More Realistic Cost Curves

Cost of unit


Quantity

## ECONOMICS IN ACTION

## Don't Put Out the Welcome Mat

- With our abundant supply of undeveloped land, real estate developers have long found it profitable to buy big parcels of land, build a large number of homes, and create entire new communities.
- But what is profitable for developers is not necessarily good for the existing residents.


## ECONOMICS IN ACTION

## Don't Put Out the Welcome Mat

- In the past few years, real estate developers have encountered increasingly stiff resistance from local residents because of the additional costs-the marginal costs-imposed on existing homeowners from new developments.
- The local tax rate that new homeowners pay on their new homes is the same as what existing homeowners pay on their older homes.
- That tax rate reflects the current total cost of services, and the taxes that an average homeowner pays reflect the average total cost of providing services to a household.


## ECONOMICS IN ACTION

## Don't Put Out the Welcome Mat

- The average total cost of providing services is based on the town's use of existing facilities, such as the existing school buildings, the existing number of teachers, the existing fleet of school buses, and so on.


## ECONOMICS IN ACTION

## Don't Put Out the Welcome Mat

- But when a large development of homes is constructed, those facilities are no longer adequate: new schools must be built, new teachers hired, and so on.
- The quantity of output increases.
- So the marginal cost of providing municipal services per household associated with a new, large-scale development turns out to be much higher than the average total cost per household of existing homes.
- As a result, new developments and facilities cause everyone's local tax rate to go up.


## Short-Run versus Long-Run Costs

- In the short run, fixed cost is completely outside the control of a firm. But all inputs are variable in the long run: This means that in the long run fixed cost may also be varied.
- In the long run, in other words, a firm's fixed cost becomes a variable it can choose.
- The firm will choose its fixed cost in the long run based on the level of output it expects to produce.


## Choosing the Level of Fixed Cost of Selena's Gourmet Salsas



## The Long-Run Average Total Cost Curve

- The long-run average total cost curve shows the relationship between output and average total cost when fixed cost has been chosen to minimize average total cost for each level of output.


## Short-Run and Long-Run Average Total Cost Curves

Cost of case

(cases)

## Returns to Scale

- There are increasing returns to scale (economies of scale) when long-run average total cost declines as output increases.
- There are decreasing returns to scale (diseconomies of scale) when long-run average total cost increases as output increases.
- There are constant returns to scale when long-run average total cost is constant as output increases.


## Summing Up Costs

table 11-3 Concepts and Measures of Cost

| Short run | Measurement | Definition | Mathematical term |
| :---: | :---: | :---: | :---: |
|  | Fixed cost | Cost that does not depend on the quantity of output produced | FC |
|  | Average fixed cost | Fixed cost per unit of output | $A F C=F C / Q$ |
| Short run and long run | Variable cost | Cost that depends on the quantity of output produced | VC |
|  | Average variable cost | Variable cost per unit of output | $A V C=V C / Q$ |
|  | Total cost | The sum of fixed cost (short run) and variable cost | $\begin{aligned} & T C=F C \text { (short run) } \\ & +V C \end{aligned}$ |
|  | Average total cost (average cost) | Total cost per unit of output | $A T C=T C / Q$ |
|  | Marginal cost | The change in total cost generated by producing one more unit of output | $M C=\Delta T C / \Delta Q$ |
| Long run | Long-run average total cost | Average total cost when fixed cost has been chosen to minimize average total cost for each level of output | LRATC |

## ECONOMICS IN ACTION

## There's No Business Like Snow Business

- Anyone who has lived both in a snowy city, like Chicago, and in a city that only occasionally experiences significant snowfall, like Washington, D.C., is aware of the differences in total cost that arise from making different choices about fixed cost.
- In Washington, even a minor snowfall-say, an inch or two overnight-is enough to create chaos during the next morning's commute.
- The same snowfall in Chicago has hardly any effect at all.
- The reason is not that Washingtonians are wimps and Chicagoans are made of sterner stuff; it is that Washington, where it rarely snows, has only a fraction as many snowplows and other snow-clearing equipment as cities where heavy snow is a fact of life.


## ECONOMICS IN ACTION

## There's No Business Like Snow Business

- In this sense Washington and Chicago are like two producers who expect to produce different levels of output, where the "output" is snow removal.
- Washington, which rarely has significant snow, has chosen a low level of fixed cost in the form of snow-clearing equipment.
- This makes sense under normal circumstances but leaves the city unprepared when major snow does fall.
- Chicago knows that it will face lots of snow so chooses to accept the higher fixed cost that leaves it in a position to respond effectively.


## Summary

1. The relationship between inputs and output is a producer's production function.

In the short run, the quantity of a fixed input cannot be varied but the quantity of a variable input can.

In the long run, the quantities of all inputs can be varied.

For a given amount of the fixed input, the total product curve shows how the quantity of output changes as the quantity of the variable input changes.

## Summary

2. There are diminishing returns to an input when its marginal product declines as more of the input is used, holding the quantity of all other inputs fixed.
3. Total cost is equal to the sum of fixed cost, which does not depend on output, and variable cost, which does depend on output.

## Summary

4. Average total cost, total cost divided by quantity of output, is the cost of the average unit of output, and marginal cost is the cost of one more unit produced.

U-shaped average total cost curves are typical, because average total cost consists of two parts: average fixed cost, which falls when output increases (the spreading effect), and average variable cost, which rises with output (the diminishing returns effect).

## Summary

5. When average total cost is $U$-shaped, the bottom of the $U$ is the level of output at which average total cost is minimized, the point of minimum-cost output.

This is also the point at which the marginal cost curve crosses the average total cost curve from below.

## Summary

6. In the long run, a producer can change its fixed input and its level of fixed cost.

The long-run average total cost curve shows the relationship between output and average total cost when fixed cost has been chosen to minimize average total cost at each level of output.
7. As output increases, there are increasing returns to scale if long-run average total cost declines; decreasing returns to scale if it increases; and constant returns to scale if it remains constant. Scale effects depend on the technology of production.

## KEY TERMS

- Production function
- Fixed input
- Variable input
- Long run
- Short run
- Total product curve
- Marginal product
- Diminishing returns to an input
- Fixed cost
- Variable cost
- Total cost
- Total cost curve
- Average total cost
- Average cost
- U-shaped average total cost curve
- Average fixed cost
- Average variable cost
- Minimum-cost output
- Long-run average total cost curve
- Increasing returns to scale
- Decreasing returns to scale
- Constant returns to scale

