Bulk viscosity of baryonic matter with trapped neutrinos and its application to neutron star mergers

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Based on: arXiv:1907.04192





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Justus-Liebig-Universität Gießen, October 23, 2019

- Introduction & motivation
- Urca processes and bulk viscosity

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- Density functional theory
- Results for bulk viscosity
- Conclusions



The structure of a neutron star



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Compact-star binaries

- Compact stars are natural laboratories which allow us to study the properties of nuclear matter under extreme physical conditions (strong gravity, strong magnetic fields, etc.).
- The recent detection of gravitational and electromagnetic waves originating from black hole or neutron star mergers motivates studies of compact binary systems.
- Such studies might place constraints on the properties of compact star parameters and contain useful information about the properties of extremely hot and dense matter.
- Various physical processes in the compact binary systems can be modelled in the framework of general-relativistic hydrodynamics simulations.
- Transport coefficients are key inputs in hydrodynamic modelling of compact star mergers as they measure the energy dissipation rate in hydrodynamic evolution of matter.
- The bulk viscosity might affect the hydrodynamic evolution of mergers by damping the density oscillations which can affect the form of the gravitational signal.

- Our aim is to study the bulk viscosity in dense baryonic matter for temperatures relevant to neutron star mergers and supernovas $T \ge 5$ MeV.
- At these temperatures neutrinos are trapped in matter, and the bulk viscosity arises from weak interaction (neutron decay and electron capture) processes.

Relativistic hydrodynamics and bulk viscosity

 Hydrodynamic evolution of a relativistic system is described by means of the energy-momentum tensor and particle current which obey the conservation laws

$$\partial_{\mu}T^{\mu\nu} = 0, \qquad \partial_{\mu}N^{\mu} = 0.$$

• For ideal hydrodynamic, i.e., without dissipation

$$T_0^{\mu\nu} = \epsilon_0 u^{\mu} u^{\nu} - p_0 \Delta^{\mu\nu}, \qquad N_0^{\mu} = n_0 u^{\mu},$$

and the system of conservation laws is closed by an equation of state p₀ = p_{eq}(ε₀, n₀).
For a dissipative fluid with velocity gradients

$$T^{\mu\nu} = \epsilon u^{\mu}u^{\nu} - p\Delta^{\mu\nu} + \pi^{\mu\nu}, \qquad N^{\mu} = nu^{\mu}.$$

• In this case the pressure obtains a non-equilibrium contribution

$$p = p_{eq} + \Pi.$$

where the bulk viscous pressure reads $\Pi = -\zeta \theta$ with $\theta = \partial_{\mu} u^{\mu}$.

 Thus, the bulk viscosity ζ describes dissipation in the case where pressure falls out of equilibrium on uniform expansion/contraction.

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Literature on bulk viscosity

- R. F. Sawyer, Damping of neutron star pulsations by weak interaction processes, Astrophys. J. 237 (1980) 187-197.
- R. F. Sawyer, Bulk viscosity of hot neutron-star matter and the maximum rotation rates of neutron stars, Phys. Rev. D 39 (1989) 3804-3806.
- P. Haensel and R. Schaeffer, Bulk viscosity of hot-neutron-star matter from direct URCA processes, Phys. Rev. D 45 (1992) 4708-4712.
- P. B. Jones, Bulk viscosity of neutron-star matter, Phys. Rev. D 64 (2001) 084003.
- M. G. Alford, S. Mahmoodifar and K. Schwenzer, Large amplitude behavior of the bulk viscosity of dense matter, Journal of Physics G Nuclear Physics 37 (2010) 125202, [1005.3769].
- M. G. Alford, L. Bovard, M. Hanauske, L. Rezzolla and K. Schwenzer, *Viscous Dissipation and Heat Conduction in Binary Neutron-Star Mergers, Physical Review Letters* 120 (2018) 041101, [1707.09475].
- D. G. Yakovlev, M. E. Gusakov and P. Haensel, Bulk viscosity in a neutron star mantle, Mon. Not. RAS 481 (2018) 4924-4930, [1809.08609].
- A. Schmitt and P. Shternin, Reaction rates and transport in neutron stars, The Physics and Astrophysics of Neutron Stars 457 (2018) 455-574 [1711.06520].
- M. Alford and S. Harris, Damping of density oscillations in neutrino-transparent nuclear matter, Phys. Rev. C 100 (2019) 035803, [1907.03795].

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Urca process rates

• We consider a simple composition of baryonic matter consisting of neutrons, protons, electrons and neutrinos. The simplest weak-interaction processes are the following (direct) Urca processes

$$n \rightleftharpoons p + e^{-} + \bar{\nu}_{e} \qquad (neutron \ decay \ process) \qquad (1)$$

$$p + e^- \rightleftharpoons n + \nu_e$$
 (electron capture process) (2)

• In β -equilibrium the chemical potentials of particles obey the relation $\mu_n + \mu_\nu = \mu_p + \mu_e$. Out of β -equilibrium in general implies an imbalance

$$\mu_{\Delta} \equiv \mu_n + \mu_{\nu} - \mu_p - \mu_e \neq 0.$$

as a measure of deviation from β -equilibrium. The rate at which μ_{Δ} relaxes to zero is a measure of speed at which the constitution of matter adjusts to a change in pressure. • The β -equilibration rate for the neutron decay is given by

$$\Gamma_{1p}(\mu_{\Delta}) = \int d\Omega \sum_{s_i} |\mathcal{M}_{Urca}|^2 f(p') \bar{f}(k') \bar{f}(p) (2\pi)^4 \, \delta^{(4)}(p+k+k'-p'),$$

with $\overline{f}(p) = 1 - f(p)$. Similar expressions can be written also for Γ_{1n} , Γ_{2p} and Γ_{2n} . • The squared matrix element of Urca processes is $[G^2 = G_F^2 \cos^2 \theta_c (1 + 3g_A^2)]$

$$\sum_{s_i} |\mathcal{M}_{Urca}|^2 = 32G^2(k \cdot p')(p \cdot k') \simeq 32G^2 p_0 p'_0 k_0 k'_0.$$

Density oscillations in neutron-star matter

• Consider now small-amplitude density oscillations in baryonic matter with frequency ω

$$n_B(t) = n_{B0} + \delta n_B(t), \quad n_L(t) = n_{L0} + \delta n_L(t), \quad \delta n_B(t), \ \delta n_L(t) \sim e^{i\omega t}.$$

• The baryon and lepton number conservation $\partial n_i / \partial t + \operatorname{div}(n_i \mathbf{v}) = 0$ implies

$$\delta n_i(t) = -\frac{\theta}{i\omega} n_{i0}, \quad i = \{B, L\}, \quad \theta = \operatorname{div} v.$$

The oscillations cause perturbations in particle densities n_j(t) = n_{j0} + δn_j(t), due to which the chemical equilibrium of matter is disturbed leading to a small shift μ_Δ = δμ_n + δμ_ν − δμ_e, which can be written as

$$\mu_{\Delta} = (A_{nn} - A_{pn})\delta n_n + A_{\nu\nu}\delta n_{\nu} - (A_{pp} - A_{np})\delta n_p - A_{ee}\delta n_e, \qquad A_{ij} = \left(\frac{\partial \mu_i}{\partial n_j}\right)_0.$$

- The off-diagonal elements *A_{np}* and *A_{pn}* are non-zero because of the cross-species strong interaction between neutrons and protons.
- If the weak processes are turned off, then a perturbation conserves all particle numbers

$$\frac{\partial}{\partial t}\delta n_j(t) + \theta n_{j0} = 0, \qquad \delta n_j(t) = -\frac{\theta}{i\omega} n_{j0}.$$

Chemical balance equations and bulk viscosity

• Out of equilibrium the chemical equilibration rate to linear order in μ_{Δ} is given by

$$\Gamma_p - \Gamma_n = \lambda \mu_\Delta, \quad \lambda > 0.$$

• The rate equations which take into account the loss and gain of particles read as

$$\frac{\partial}{\partial t}\delta n_n(t) + \theta n_{n0} = -\lambda \mu_{\Delta}(t), \qquad \frac{\partial}{\partial t}\delta n_p(t) + \theta n_{p0} = \lambda \mu_{\Delta}(t).$$

• Solving these equations we can compute the pressure out of equilibrium

$$p = p(n_j) = p(n_{j0} + \delta n_j) = p_0 + \delta p = p_{eq} + \delta p',$$

where the non-equilibrium part of the pressure - the bulk viscous pressure, is given by

$$\Pi \equiv \delta p' = \sum_{j} \left(\frac{\partial p}{\partial n_{j}}\right)_{0} \delta n'_{j} = \sum_{ij} n_{i0} A_{ij} \delta n'_{j}.$$

• The bulk viscosity is then identifined from $\Pi = -\zeta \theta$

$$\zeta = \frac{C^2}{A} \frac{\lambda A}{\omega^2 + \lambda^2 A^2}$$

with susceptibilities $A = -\frac{1}{n_B} \left(\frac{\partial \mu_{\Delta}}{\partial x_p} \right)_{n_B}$ and $C = n_B \left(\frac{\partial \mu_{\Delta}}{\partial n_B} \right)_{x_p}$.

Limiting cases for bulk viscosity

• In the low-temperature limit the matter is ν -transparent, and the equilibration rate λ reads

$$\lambda_{\text{trans}} = \frac{17}{240\pi} m^{*2} G^2 T^4 p_{Fe} \theta(p_{Fp} + p_{Fe} - p_{Fn}),$$

where p_{Fi} are Fermi-momenta of particles. The θ -function blocks direct Urca processes at densities where $p_{Fp} + p_{Fe} < p_{Fn} \Rightarrow modified Urca processes should be included.$

• The neutrino-trapped β -equilibration rate for strongly degenerate matter is given by

$$\lambda_{\text{trap}} = \frac{1}{12\pi^3} m^{*2} G^2 T^2 p_{Fe} p_{F\nu} (p_{Fe} + p_{F\nu} - |p_{Fn} - p_{Fp}|).$$

In contrast to the ν -transparent case here the rate is finite in the low-temperature limit \Rightarrow modified Urca reactions are not required to be included.

- Because in the degenerate regime $p_{Fi} \gg T$, the equilibration rate is alwals much larger in the case of trapped neutrinos.
- In the high-frequency ($\omega \gg \lambda A$), low-frequency ($\omega \ll \lambda A$) limits and at the maximum of the bulk viscosity ($\omega = \lambda A$) we find

$$\zeta_{\text{high}} = \frac{C^2 \lambda}{\omega^2}, \qquad \zeta_{\text{low}} = \frac{C^2}{\lambda A^2}, \qquad \zeta_{\text{max}} = \frac{C^2}{2A\omega}.$$

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Beta-equilibrated nuclear matter

We use the density functional theory approach to the nuclear matter, which is based on phenomenological baryon-meson Lagrangians of the type proposed by Walecka and others.

The Lagrangian density of matter is given by

$$\mathcal{L} = \sum_{N} \bar{\psi}_{N} \left[\gamma^{\mu} \left(i\partial_{\mu} - g_{\omega N}\omega_{\mu} - \frac{1}{2}g_{\rho N}\boldsymbol{\tau}\boldsymbol{\rho}_{\mu} \right) - m_{N}^{*} \right] \psi_{N} + \sum_{\lambda} \bar{\psi}_{\lambda} (i\gamma^{\mu}\partial_{\mu} - m_{\lambda})\psi_{\lambda} + \frac{1}{2}\partial^{\mu}\sigma\partial_{\mu}\sigma - \frac{1}{2}m_{\sigma}^{2}\sigma^{2} - U(\sigma) - \frac{1}{4}\omega^{\mu\nu}\omega_{\mu\nu} + \frac{1}{2}m_{\omega}^{2}\omega^{\mu}\omega_{\mu} - \frac{1}{4}\boldsymbol{\rho}^{\mu\nu}\boldsymbol{\rho}_{\mu\nu} + \frac{1}{2}m_{\rho}^{2}\boldsymbol{\rho}^{\mu}\boldsymbol{\rho}_{\mu}.$$

The pressure of baryonic matter is given by

$$P_{N} = -\frac{m_{\sigma}^{2}}{2}\sigma^{2} - U(\sigma) + \sum_{\lambda} \frac{g_{\lambda}}{6\pi^{2}} \int_{0}^{\infty} \frac{k^{4} dk}{(k^{2} + m_{\lambda}^{2})^{1/2}} \left[f(E_{k}^{\lambda} - \mu_{\lambda}) + f(E_{k}^{\lambda} + \mu_{\lambda}) \right] \\ + \frac{m_{\omega}^{2}}{2}\omega_{0}^{2} + \frac{m_{\rho}^{2}}{2}\rho_{03}^{2} + \sum_{N} \frac{2J_{N} + 1}{6\pi^{2}} \int_{0}^{\infty} \frac{k^{4} dk}{(k^{2} + m_{N}^{*2})^{1/2}} \left[f(E_{k}^{N} - \mu_{N}^{*}) + f(E_{k}^{N} + \mu_{N}^{*}) \right]$$

Here $m_N^* = m_N - g_{\sigma N}\sigma$ and $\mu_N^* = \mu_N - g_{\omega N}\omega_0 - g_{\rho N}\rho_{03}I_3$ are the nucleon effective mass and effective chemical potentials, respectively; I_3 is the third component of nucleon isospin and σ , ω_0 and ρ_{03} are the mean values of the meson fields. Density functional theory

Meson mean-fields and susceptibilities

• The mean-field values of the ω and ρ mesons are given by

$$g_{\omega}\omega_0 = \left(\frac{g_{\omega}}{m_{\omega}}\right)^2 (n_n + n_p), \qquad g_{\rho}\rho_{03} = \frac{1}{2}\left(\frac{g_{\rho}}{m_{\rho}}\right)^2 (n_p - n_n).$$

The mean value of the scalar field is given by

$$g_{\sigma}\sigma = -\frac{g_{\sigma}}{m_{\sigma}^2}\frac{\partial U(\sigma)}{\partial \sigma} + \frac{1}{\pi^2}\left(\frac{g_{\sigma}}{m_{\sigma}}\right)^2 \sum_N \int_0^\infty p^2 dp \frac{m^*}{\sqrt{p^2 + m^{*2}}} [f_N(p) + \bar{f}_N(p)].$$

• The "beta-disequilibrium-proton-fraction" susceptibility in low-T limit is given by

$$A = \frac{\pi^2}{m^*} \left(\frac{1}{p_{Fn}} + \frac{1}{p_{Fn}} \right) + \frac{\pi^2}{p_{Fe}^2} + \frac{2\pi^2}{p_{F\nu}^2} + \left(\frac{g_{\rho}}{m_{\rho}} \right)^2$$

• The "beta-disequilibrium-baryon-density" susceptibility in low-T limit reads

$$C = \frac{p_{Fn}^2 - p_{Fp}^2}{3m^*} + \frac{p_{F\nu} - p_{Fe}}{3} + \frac{n_n - n_p}{2} \left(\frac{g_{\rho}}{m_{\rho}}\right)^2 + n_B \frac{p_{Fn}^2 - p_{Fp}^2}{2m^{*2}} \left(\frac{g_{\sigma}}{m_{\sigma}}\right)^2$$

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Particle fractions in equilibrium

The particle fractions are found from β -equilibrium conditions $\mu_n + \mu_\nu = \mu_p + \mu_e$ and $\mu_\mu = \mu_e$, the charge neutrality condition $n_p = n_e + n_\mu$, the baryon number conservation $n_B = n_n + n_p$, and the lepton number conservation $n_l + n_{\nu_l} = n_L = Y_L n_B$.



• We consider two cases: (i) $Y_L = 0.1$ for both flavors, typical for neutron star mergers; (ii) $Y_{L_e} = 0.4$ and $Y_{L_{\mu}} = 0$ typical for matter in supernovae and proto-neutron stars.

- The particle fractions are not sensitive to the temperature for the given value of Y_L .
- In the low-density and high-temperature regime the net neutrino density becomes negative, indicating that there are more anti-neutrinos than neutrinos in that regime.
- Merger matter has much smaller electron neutrino fraction than supernova matter.

Density functional theory

The equation of state for two models of nuclear matter



- In the case of model DD-ME2 $U(\sigma) = 0$, and the couplings g_{σ} , g_{ω} and g_{ρ} are density-dependent.
- In the case of model NL3 $U(\sigma) = g_2 \sigma^3 / 3 + g_3 \sigma^4 / 4 \neq 0$, but the couplings g_σ , g_ω and g_ρ are density-independent.

β -equilibration rates (DD-ME2)



- The neutron decay rate Γ₁ is exponentially suppressed at low temperatures because of damping of anti-neutrino population in the degenerate matter.
- The electron capture rate Γ_2 has a finite low-temperature limit which is $\propto T^3$.
- In the regime of interest $\Gamma_1 \ll \Gamma_2$, therefore the electron capture process dominates in the β -equilibration and the bulk viscosity.

β -relaxation rate (DD-ME2)



- The β -relaxation rate λA determines the frequency at which the bulk viscosity reaches its resonant maximum ($\omega_{max} = \lambda A$).
- The relaxation rate is slowest in the neutrino-transparent case, and increases with the lepton fraction in the neutrino-trapped case.
- In neutrino-trapped matter $\lambda A \gg \omega$ for oscillation frequencies typical to neutron star mergers and supernovas \Rightarrow the bulk viscosity takes the form $\zeta \approx C^2/(\lambda A^2)$.
- The neutrino-transparent matter instead features a relaxation rate which is comparable to the oscillation frequencies at typical temperatures $T \simeq 2 \div 7$ MeV.

The susceptibility prefactor C^2/A (DD-ME2)



- The susceptibility A does not depend strongly on the density and temperature and has roughly the same order of magnitude $A \sim 10^{-3} \text{ MeV}^{-2}$.
- The susceptibility C increases with density and at high temperatures $T \gtrsim 30 \text{ MeV}$ crosses zero at certain values of density where the proton fraction attains a minimum.
- At this critical density the system is scale-invariant: it can be compressed and remain in beta equilibrium ⇒ the bulk viscosity drops to zero at the critical point.

Bulk viscosity of neutrino-trapped matter (DD-ME2)



- The density dependence of the bulk viscosity follows that of the susceptibility C^2/A .
- The temperature dependence of ζ arises mainly from that of β -relaxation rate $\lambda A \propto T^2$.
- Bulk viscosity is independent of oscillation fequency and decreases as $\zeta \propto T^{-2}$ in the neutrino-trapped regime.
- This scaling breaks down at high temperatures $T \ge 30$ MeV where the bulk viscosity has sharp minimums $\zeta \to 0$ when the matter becomes scale-invariant.

Bulk viscosity of neutrino-trapped matter (NL3)



- The density dependence of the bulk viscosity follows that of the susceptibility C^2/A .
- The temperature dependence of ζ arises mainly from that of β -relaxation rate $\lambda A \propto T^2$.
- Bulk viscosity is independent of oscillation fequency and decreases as $\zeta \propto T^{-2}$ in the neutrino-trapped regime.
- This scaling breaks down at high temperatures $T \ge 30$ MeV where the bulk viscosity has sharp minimums $\zeta \to 0$ when the matter becomes scale-invariant.

Bulk viscosity of neutrino-transparent matter



- The bulk viscosity in neutrino-transparent matter is frequency-dependent.
- The relaxation rate is slower for neutrino-transparent matter, and the resonant peak of the bulk viscosity occurs within its regime of validity.
- It attains its maximum value at temperature $T \simeq 2 \div 7$ MeV, where $\omega = \lambda A$.
- This is the temperature range which is relevant for neutron-star mergers. ¹

¹M. G. Alford, et al., On the importance of viscous dissipation and heat conduction in binary neutron-star mergers, 2017 🔊 🗟

Bulk viscosity of neutrino-transparent matter (NL3)



- The bulk viscosity in neutrino-transparent matter is frequency-dependent.
- The relaxation rate is slower for neutrino-transparent matter, and the resonant peak of the bulk viscosity occurs within its regime of validity.
- It attains its maximum value at temperature $T \simeq 2 \div 7$ MeV, where $\omega = \lambda A$.
- This is the temperature range which is relevant for neutron-star mergers.²

²M. G. Alford, *et al.*, On the importance of viscous dissipation and heat conduction in binary neutron-star mergers, 2017 🖉 🔗 🔍

Bulk viscosity of baryonic matter (DD-ME2)



- We interpolate our numerical results for the bulk viscosity between the neutrino-transparent and neutrino-trapped regimes in the interval 5 ≤ T ≤ 10 MeV.
- The bulk viscosity in the neutrino transparent regime is larger, and drops by orders of magnitude as the matter enters the neutrino-trapped regime.
- The bulk viscosity attains its maximum at temperatures $T \simeq 2 \div 6$ MeV.

Bulk viscosity of baryonic matter (NL3)



- We interpolate our numerical results for the bulk viscosity between the neutrino-transparent and neutrino-trapped regimes in the interval 5 ≤ T ≤ 10 MeV.
- The bulk viscosity in the neutrino transparent regime is larger, and drops by orders of magnitude as the matter enters the neutrino-trapped regime.
- The bulk viscosity attains its maximum at temperatures $T \simeq 2 \div 6$ MeV.

Estimation of oscillation damping timescale

• The energy density of baryonic oscilations with amplitude δn_B is

$$\epsilon = \frac{K}{2} \frac{(\delta n_B)^2}{n_B}.$$

• Coefficient *K* is the compressibility of nuclear matter

$$K=n_B\frac{\partial^2\varepsilon}{\partial n_B^2}.$$

• The enegy dissipation rate per volume by bulk viscosity is

$$\frac{d\epsilon}{dt} = \frac{\omega^2 \zeta}{2} \left(\frac{\delta n_B}{n_B}\right)^2$$

• The characteristic timescale required for dissipation is $\tau = \epsilon/(d\epsilon/dt)$

$$\tau = \frac{Kn_B}{\omega^2 \zeta}$$

In the high-frequency (ω ≫ λA), low-frequency (ω ≪ λA) limits and at the maximum of the bulk viscosity (ω = λA) we find

$$\tau_{\rm high} = \frac{Kn_B}{\lambda C^2}, \qquad \tau_{\rm low} = \frac{\lambda^2 A^2}{\omega^2} \frac{Kn_B}{\lambda C^2}, \qquad \tau_{\rm min} = 2 \frac{Kn_B}{\lambda C^2}.$$

Nuclear compressibility for two EoS



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Oscillation damping timescale for DD-ME2 model



- Damping timescales are comparable to the merging timescales $\tau_{\text{merg}} \simeq 10 \text{ ms}$ at temperatures $T \lesssim 7 \text{ MeV}$ where neutrinos are not trapped.
- Therefore, bulk viscosity will have its greatest impact on neutron star mergers in regions that are neutrino transparent rather than neutrino trapped.
- This also implies weak damping of gravitational waves emitted by the oscillations of the post-merger remnant in the high-temperature, neutrino-trapped phase of evolution.

Oscillation damping timescale for NL3 model



- Damping timescales are comparable to the merging timescales $\tau_{\text{merg}} \simeq 10 \text{ ms}$ at temperatures $T \lesssim 7 \text{ MeV}$ where neutrinos are not trapped.
- Therefore, bulk viscosity will have its greatest impact on neutron star mergers in regions that are neutrino transparent rather than neutrino trapped.
- This also implies weak damping of gravitational waves emitted by the oscillations of the post-merger remnant in the high-temperature, neutrino-trapped phase of evolution.

Conclusions

Conclusions

- We studied the bulk viscosity of dense nuclear matter in the case of trapped neutrinos.
- We find that the bulk viscosity is dominated by electron capture process and its inverse.
- The bulk viscosity attains its maximum at temperatures 2 ÷ 7 MeV for neutrino-transparent matter.
- The neutrino-trapped bulk viscosity does not attain its maximum within its range of validity because of faster equilibration rates.
- The nuclear matter becomes scale-invariant at a critical density at high temperatures $T \ge 30$ MeV driving the bulk viscosity to zero at those points.
- The bulk viscosity of neutrino-trapped matter is several orders of magnitude smaller than that of neutrino-transparent matter.
- We find that the neutron star oscillation damping timescales in neutrino-trapped matter are likely to be too long to affect the evolution of neutron star mergers.
- This also implies weak damping of gravitational waves emitted by the oscillations of the post-merger remnant in the high-temperature, neutrino-trapped phase of evolution.

THANK YOU FOR ATTENTION!