

Quark masses and mixings in a minimally parameterised ultraviolet completion of the Standard Model

Quark masses and CKM determined by RG FPs?

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... to appear soon ...

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*Quark masses and mixings in a minimal, parameterized
ultraviolet completion of the Standard Models,*

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A few facts about the Standard Model

The Standard Model of particle physics (SM) comprises:

- ▶ **22.5 [24] Dirac fermions, 4 scalars, 12 gauge bosons = vectors**
SM dominated by fermions: no SUSY, Pauli sum rules violated, etc.
- ▶ U(1), SU(2) & SU(3) gauge, Higgs & Yukawa **interactions**
SU(2) and SU(3) gauge interactions asymptotically free
- ▶ ... many (>20) parameters ...
Determined to a high precision by many experiments!
Only an “aesthetic” problem?
- ▶ Huge differences between masses & complicated mixing patterns!
Flavour puzzle!!!
- ▶ Triviality problem (Landau’s zero charge), resp., Landau poles
SM is an Effective Field Theory!!!



A modern perception of QFTs: The EFT paradigm?

At each energy scale:

- Model (i.e., a QFT) for observed d.o.f. & symmetries;
- in principle infinitely many parameters but only “a few” relevant for observables.
- Threshold at some higher mass scale:
update the model!
- No need for a well-defined UV limit!
- Conversely: Fundamental theory is “shielded” from observation.

A paradigm change? Or,

why is the Higgs $m_H=125$ GeV so special?

If it were

- larger \Rightarrow low-scale Landau pole!
- smaller \Rightarrow vacuum instability!¹

$m_H=125$ GeV: SM is theoretically viable at much higher scales.

Nevertheless: Transplanckian Landau poles,
new physics at high scales has to exist.

¹ cf., Higgs mass prediction of Shaposhnikov & Wetterich.

For the presented investigation we assume:

A modification of the β -function of the Abelian gauge coupling

$$\beta_Y = \beta_Y^{SM} - f_g g_Y, \quad f_g = \begin{cases} 0, & k < M_{NP} \\ \text{const}, & k \geq M_{NP}, \end{cases}$$

and analogously for all Yukawa couplings,

$$\beta_{y_i} = \beta_{y_i}^{SM} - f_y y_i, \quad i \in \{d, u, s, c, b, t\}, \quad f_y = \begin{cases} 0, & k < M_{NP} \\ \text{const}, & k \geq M_{NP}, \end{cases}$$

with M_{NP} at or close to the Planck scale $\propto 1/\sqrt{8\pi G_N}$.

NB: 1. M_{NP} can thus be also a GUT scale.

2. Includes assuming no (or only little) new physics up to M_{NP} .

UV completion from Asymptotically Safe Gravity

Evidence for an interacting UV fixed point in gravity:

- Viable theory of quantum gravity
(Asymptotically Safe Quantum Gravity)
- Verified for Einstein-Hilbert, $f(R)$, . . . gravity
- Coupling of SM matter: Quantitative but no qualitative changes

Impact of quantum-gravity fluctuations on SM matter:

QUANTUM-GRAVITY INDUCED UV COMPLETION!

such that leading-order terms are parameterized by form above.

- 1.) $f_g > 0$ (i.e., anti-screening) from positive G_N .
- 2.) One universal (“flavour-blind”) f_y , sign undetermined.



Note that this is only an example!

Minimal parameterization of BSM physics:

Within this approach one can stay completely agnostic but novel fields and/or additional symmetries of the new physics!

In this talk: Neglect leptons.

Use one-loop (two-loop) expressions for SM β -functions + postulated linear terms:

- Zeros of the β -functions: Fixed Points
- Gaußian and interacting FPs possible
- UV and IR FPs
- Permutation Symmetry S_3 of up-type and down-type quarks
 - S_3 symmetric FP:
Different values of the Yukawa couplings due to RG flow.
 - Multiplet of FPs:
Additional symmetry breaking by choice of FP.

- *New-physics contribution drops out of the running of CKM.*
The corresponding SM IR attractive fixed point persists.
This fixed point dominates the IR physics of the CKM matrix.
- Unitarity of the CKM matrix:
non-polynomial β -functions for the mixing angles.
- Singular for identical Yukawa couplings! (see below)
- No FPs with finite / non-vanishing equal up-type (down-type) Yukawa couplings.
- Starting from a FP which is member of a multiplet:
Neither the three up- nor the three down-type quarks can have equal masses.
- Poles in β -functions limits the values of the masses in the flow and thus in the IR.

FPs & RG flow for one generation

Non-Abelian gauge couplings asymptotically free: $g_{2*} = 0 = g_{3*}$.

Eight FPs:

Four with asymp. free Abelian gauge coupling,
four interacting ones s.t. $g_{Y*} = 4\pi\sqrt{6f_g/41}$.

All FPs fulfill:

$$y_{t*}^2 - y_{b*}^2 = \frac{1}{3}g_{Y*}^2.$$

Finite FP value for Abelian charge:

- different top and bottom masses!
- larger top mass due larger hypercharge!

Phenomenological values for top and bottom mass in IR ($k = 173\text{GeV}$).



FPs & RG flow for two generations

Best parameterization for mixing = Cabbibo matrix squared:

$$\left[\{|V_{ij}|^2\} \right] = \begin{bmatrix} W & 1 - W \\ 1 - W & W \end{bmatrix}$$

Corresponding β -function:

$$\beta_W = \frac{3}{16\pi^2} W (W - 1) \left[(y_t^2 + y_c^2) \frac{y_b^2 - y_s^2}{y_t^2 - y_c^2} + (y_b^2 + y_s^2) \frac{y_t^2 - y_c^2}{y_b^2 - y_s^2} \right]$$

System of β -functions:

20 FPs and two lines of FPs in one-loop truncation²,

24 FPs in two-loop truncation,

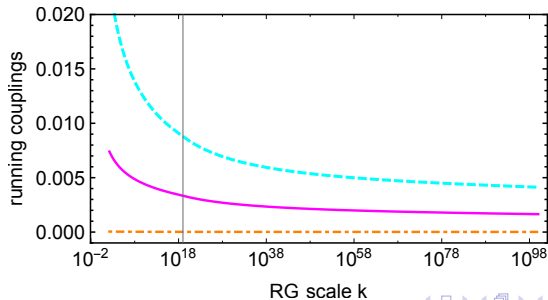
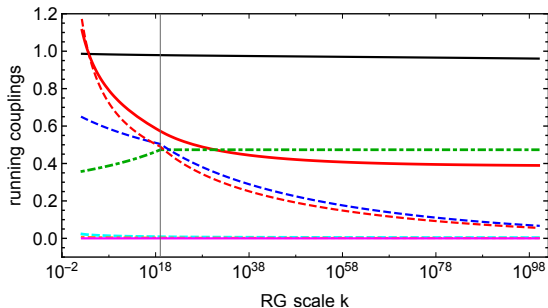
grouped in six quartets.

²RG invariant combinations of couplings at one-loop level

Structure of one quartet of FPs:

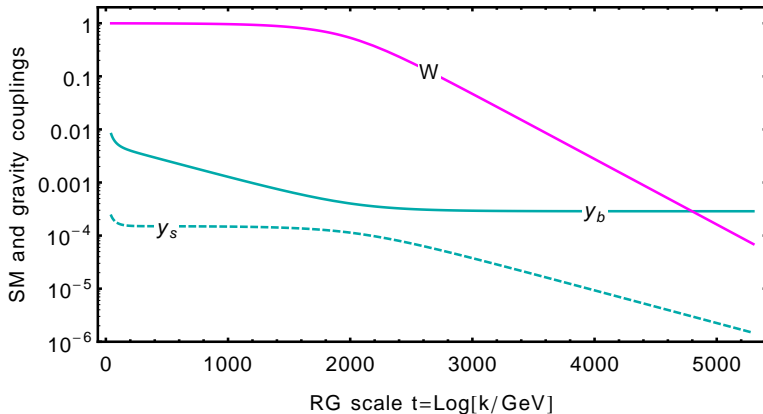
#	$y_{t^*}^2 / \left(\frac{15}{615} \pi^2\right)$	$y_{c^*}^2 / \left(\frac{15}{615} \pi^2\right)$	$y_{b^*}^2 / \left(\frac{15}{615} \pi^2\right)$	$y_{s^*}^2 / \left(\frac{15}{615} \pi^2\right)$	W_*
1a	$41 (f_g + 2f_y)$	0	$-19f_g + 82f_y$	0	0
1b	$41 (f_g + 2f_y)$	0	0	$-19f_g + 82f_y$	1
1c	0	$41 (f_g + 2f_y)$	0	$-19f_g + 82f_y$	0
1d	0	$41 (f_g + 2f_y)$	$-19f_g + 82f_y$	0	1

FPs & RG flow for two generations



FPs & RG flow for two generations

Limit on strange mass due to singularity:



For FP 1a and $f_g = 9.7 \cdot 10^{-3}$, $f_y = 2.248 \cdot 10^{-3}$,

at $k = 173$ GeV:

- All three gauge couplings correct.
- $W \approx 0.999$.
- $M_t \approx 193$ GeV, $M_b \approx 4.2$ GeV, $M_c \approx 1.3$ GeV and $M_s \approx 97$ MeV.

I.e., besides an overestimated top mass astonishingly well reproduced SM parameters.

System has more than 1000 FPs!

Use the heavy-top limit to screen for phenomenologically viable FPs and solve then the flow for the full system.

FPs & RG flow for three generations

Parameterization of mixing:

$$\left[\{|V_{ij}|^2\} \right] = \begin{bmatrix} X & Y & 1 - X - Y \\ Z & W & 1 - Z - W \\ 1 - X - Z & 1 - Y - W & X + Y + Z + W - 1 \end{bmatrix}$$

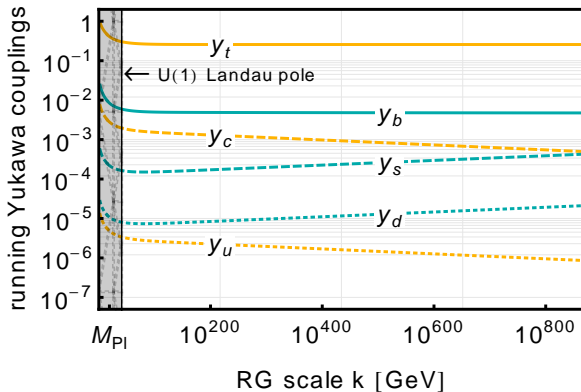
FP structure of mixing:

$$M_{123} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad M_{132} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}, \quad M_{321} = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix},$$

$$M_{213} = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad M_{312} = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}, \quad M_{231} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}$$

FPs & RG flow for three generations

A strictly viable, predictive, but not fully fundamental UV completion:

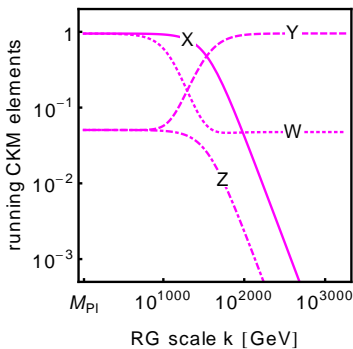
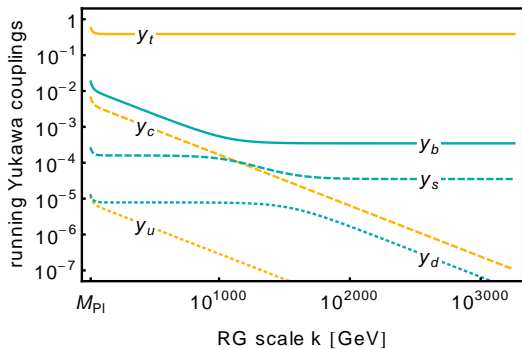


All gauge couplings, quark masses and mixings reproduced with $m_{NP} = 10^{15}$ GeV, $f_g = 8.4 \times 10^{-3}$ and $f_y = 1.4303 \times 10^{-4}$.
SM Landau pole at 10^{41} GeV shifted to 10^{1000} GeV.



FPs & RG flow for three generations

A strictly fundamental but only approximately viable UV completion:

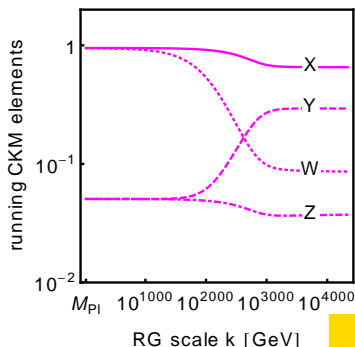
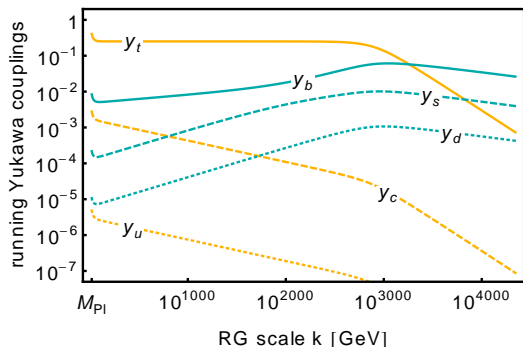


Top mass overestimated by 10%!

FPs & RG flow for three generations

A less-predictive but strictly viable and fundamental UV completion:

Use negative f_y ,
choose FP such that all Yukawa couplings are asymptotically free,
then quark masses are not predicted (IR values used as input).



Conclusions and outlook

Three main conclusions:

- New-physics contribution drops out of the running of the CKM. The corresponding **SM IR attractive fixed point** persists. This fixed point **dominates the IR physics of the CKM matrix**.
- Top and bottom masses: Predictions in qualitative agreement with phenomenology. Measured IR values of all other quarks can be accommodated (free parameters at the UV fixed point of the system).
- Interplay of CKM matrix elements and Yukawa couplings leads to **upper bounds on the free-parameter Yukawa couplings**.

Outlook:

- Include leptons.
- Θ term.
- Higher-dimensional operators.
- Explore BSM candidates.

