Consequences of a dressed quark-gluon vertex in heavy-light mesons

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Motivation

• QCD and the structure of hadrons

 \star the role of the quark masses in hadron spectrum and structure

• Heavy-light mesons

 \star Dynamics of the heavy-light meson controlled by dynamics of the heavy quark

 \star For mesons with $m_Q \sim m_M$ and $\frac{m_{\bar{q}}}{m_Q} \sim 0$: some conditions are provided by "heavy-quark symmetry"

Neubert Phys. Rept. 245 (1994)

• Heavy-quark symmetry as a guidance

 \star Use constraints of heavy-quark symmetry to check the correct behaviour of the mass

 \star Similar procedure within point-form Hamiltonian dynamics using a constituent quark model: fully relativistic treatment of light quark is necessary

Gomez-Rocha, Schweiger PRD 86 (2012)

• Limitations of BSE/DSE description of hadrons when using the rainbow-ladder truncation approach

The main goal of this work...

Based on previous studies of consequences of a dressed quark-gluon vertex in $q\bar{q}$ mesons...

Bender, Detmold, Thomas, Roberts, PRC **65** (2002) Bhagwat, Höll, Krassnigg, Roberts, Tandy PRC **70** (2004)

Use the same interaction model:

Munczek and Nemirovsky PRD 28, 181 (1983)

- sufficiently simple \rightarrow allow to compute an arbitrary number of iterations
- sufficiently realistic \rightarrow important features in common with QCD: e.g. confinement, dynamical chiral symmetry breaking
- ... attempt to generalize to $q\bar{Q}$ mesons

... ask:

Which kind of consequences do corrections to the bare vertex in heavy-light mesons have?

or...

Which kind of heavy-light physics are we "truncating" using RL approximation?

Dyson-Schwinger/Bethe-Salpeter approach The interaction model

DSE:

$$S^{-1}(p) = ip + 1m_q + \int \frac{d^4q}{(2\pi)^4} g^2 D_{\mu\nu}(p-q) \frac{\lambda^a}{2} \gamma_{\mu} S(q) \Gamma^a_{\nu}(q;p)$$

Interaction model : $\mathcal{D}_{\mu\nu}(k) := \frac{4}{3} \delta_{\mu\nu} (2\pi)^4 \mathcal{G}^2 \delta^4(k)$

Munczek and Nemirovsky PRD 28, 181 (1983)

DSE becomes an algebraic equation

- ⇒ Solvable at every truncation order: n = 0, 1, 2, 3...
- \Rightarrow Analytical solution in RL
- $\Rightarrow \text{ Solvable in the limit } n \to \infty$ (fully dressed)



figure adapted from Bender et al. PRC 65 2002

$$\Gamma^{\mathcal{C}}_{\mu,n+1}(p) = -\mathcal{C}\gamma_{\nu}S(p)\Gamma^{\mathcal{C}}_{\mu,n}(p)S(p)\gamma_{\nu}$$

Solutions to the DSE for n loops



Quark propagator: $S^{-1}(p) = ipA(p^2) + B(p^2); M(p^2) := B(p^2)/A(p^2)$

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BSE:

$$\Gamma_M(p;P) = \int \frac{d^4q}{(2\pi)^4} g^2 [\mathcal{K}(p;q;P)] \underbrace{S(q_+)\Gamma_M(q;P)S(q_-)}_{\chi_M(q;P)} \Gamma^a_\nu(q;p)$$

$$p_+ = \eta P, \quad p_- = (\eta - 1)P$$

Use an appropriate kernel that guarantees validity of Ward-Takahashi identities

Bender et al. PRC65(2002)

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Generalize to $m_q \neq m_{\bar{q}}$ and use our MN model to simplify the calculation

Dyson-Schwinger/Bethe-Salpeter approach The interaction model

Generalize to $m_q \neq m_{\bar{q}}$

$$\Gamma_{M}(p;P) = \int_{q}^{\Lambda} \mathcal{D}_{\mu\nu}(p-q) \, l^{a} \frac{1}{2} \Big[\gamma_{\mu} \chi_{M}(q;P) \, l^{a} \, \Gamma_{\nu}(q_{-},p_{-}) + \Lambda^{a}_{M\nu}(q,p;P) S(q_{-}) \gamma_{\mu} \\ + l^{a} \, \Gamma_{\nu}(q_{+},p_{+}) \chi_{M}(q;P) \gamma_{\mu} + \gamma_{\mu} S(q_{+}) \, \Lambda^{a}_{M\nu}(q,p;P) \Big],$$



figure adapted from Bender et al. PRC 65 (2002)

Derive recursion relation for $\Lambda^a_{M\nu}(q, p; P)$ for $m_q \neq m_{\bar{q}}$ \Rightarrow Corrections are more involve than for $m_q = m_{\bar{q}}$

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Search for bound-state solutions...

• Pseudoscalar mesons: $q\bar{q}, Q\bar{Q}, q\bar{Q}$

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- Vector mesons: $q\bar{q}, Q\bar{Q}, q\bar{Q}$
- Scalars \rightarrow no solution
- Axial vectors \rightarrow no solution

Solutions to the BSE

First impression for $q\bar{q}$ systems

The pion



n = # of loops

Now: check η -dependence, since this is an issue for unequal-mass constituents

(see also original MN-paper, η was used as fitting parameter).

$$\eta = \frac{p_+}{P}, \quad (\eta - 1) = \frac{p_-}{P}$$

Why η -dependence?

Because MN omits 2 of 4 covariants in BS amplitude \rightarrow this breaks Lorentz covariance: systematic error <0.8%



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Correction to RL ~ 8% for $\eta = 0.5$

Heavy quarkonia $Q\bar{Q}$



 $\begin{array}{l} \mbox{Correction to RL} \sim 1.6\% \mbox{ for } \eta = 0.5 \\ \mbox{Error due to } \eta\mbox{-dep} < 6\% \end{array}$

 $\begin{array}{l} \mbox{Correction to RL} \sim 0.2\% \mbox{ for } \eta = 0.5 \\ \mbox{Error due to } \eta\mbox{-dep} < 1.5\% \end{array}$

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 $\eta\text{-}\mathrm{dep}$ increases with increasing n

First check for mesons with $m_q \neq m_{\bar{q}}$:

Kaon



Correction to RL $\sim 7.2\%$ for $\eta = 0.5$ Error due to η -dep < 10%

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$q\bar{Q}$ -mesons



Correction to RL ~ 6.3% for $\eta = 0.75$ Error due to η -dep < 15% $m_D^{\text{full}} = 1.68 \text{ GeV}$

 $\eta\text{-}\mathrm{dep}$ decreases with increasing n

 $\begin{array}{l} \mbox{Correction to RL} \sim 3.6\% \mbox{ for } \eta = 0.95 \\ \mbox{Error due to } \eta\mbox{-dep} < 12\% \\ m_B^{\rm full} = 5.08 \mbox{ GeV} \end{array}$

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Summary

- Interest in $q\bar{Q}$ meson properties, phenomenology and structure from QCD
- Showed you an approach to these problems within DSE/BSE formalism
- Based on previous works, used an interaction model where
 - ★ Very heavy quarks and mesons can be studied numerically (even heavy-quark limit)
 - $\star~$ Effects beyond the popular RL truncation of DSE/BSE can be studied systematically and quantitatively

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$\pi\sim 8\%$	$K \sim 7.2 \ \%$
$\eta_c \sim 1.6\%$	$D\sim 6.3~\%$
$\eta_b \sim 0.2\%$	$B\sim 3.6~\%$
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BUT: η -dependence must be better understood

Conclusions and Outlook

- Setup established previously was adapted to investigate $q\bar{q},\,Q\bar{Q},\,q\bar{Q}$ meson
- Corrections to the RL truncation are more complicated in $q\bar{Q}$ mesons than in $q\bar{q}$ mesons
- Model artifacts have to be taken into account and kept under control (η -dependence)
- Heavy-light meson masses computed from the given model and parameters are reasonable
- Check heavy-quark symmetry predictions: relations between vector and pseudoscalar mesons in extreme case $m_Q \gg m_q$

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• Decay constants

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Thank you!

• Decay constants